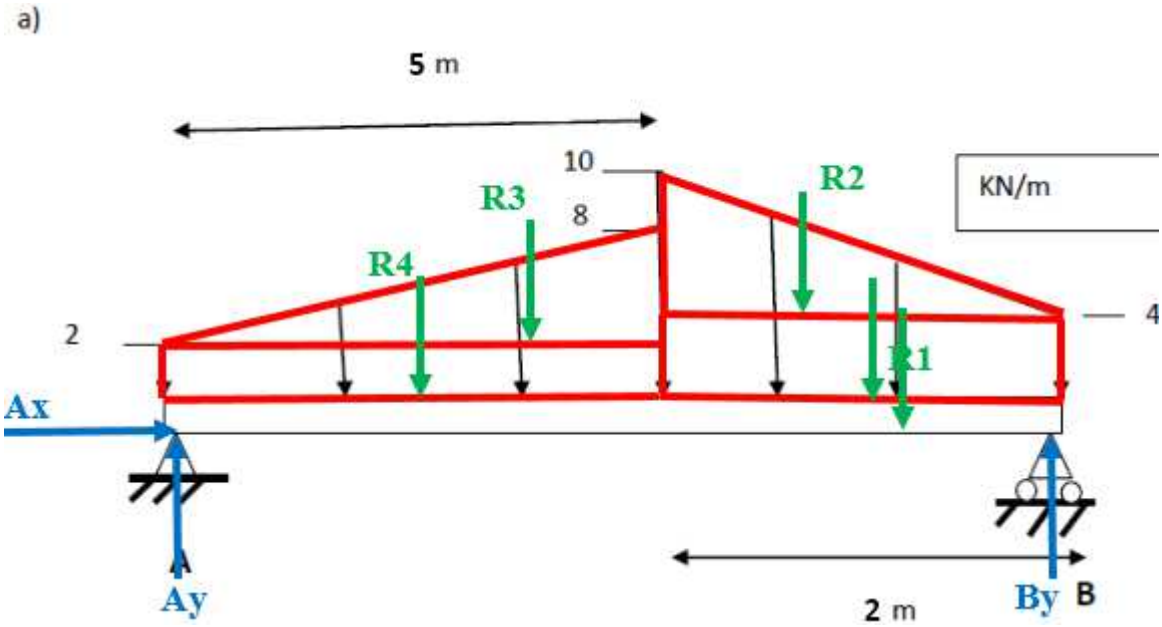
Exercice 1 :

a/



Calculons d'abord les résultantes :

Calcul de R1 :

$$R1 = 4 \times 2 = 8\ kN$$

Point d'application : $x1 = 5 + 2/2 = 6\ m\ de\ point\ A$

Calcul de R2 :

$$R2 = (10 - 4) \times 2 \times \frac{1}{2} = 6\ kN$$

Point d'application : $x2 = 5 + \frac{2}{3} = 5{,}66\ m\ de\ point\ A$

Calcul de R3 :

$$R3 = (8 - 2) \times 5 \times \frac{1}{2} = 15\ kN$$

Point d'application : $x3 = 2 \times \frac{5}{3} = \frac{10}{3}\ m\ de\ point\ A$

Calcul de R4 :

$$R4 = 2 \times 5 = 10\ kN$$

Point d'application : $x4 = 2{,}5\ m\ de\ point\ A$

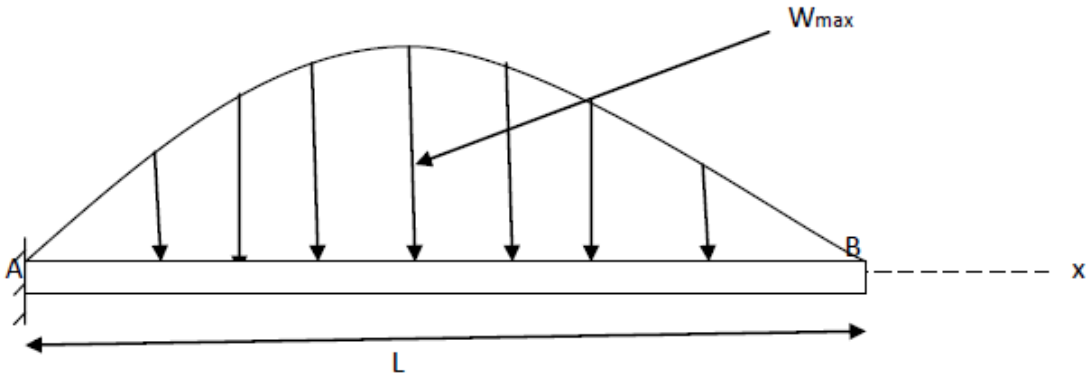
Les réactions :

$$\sum M_A = 0 \iff By \times 7 - R1 \times 6 - R2 \times 5{,}66 - R3 \times \frac{10}{3} - R4 \times 2{,}5$$
$$\Rightarrow By = 22{,}42\ kN$$

$$\sum F_y = 0 \iff Ay + By - R1 - R2 - R3 - R4 = 0$$
$$\Rightarrow Ay = 16{,}58\ kN$$

Et $Ax = 0$

b/



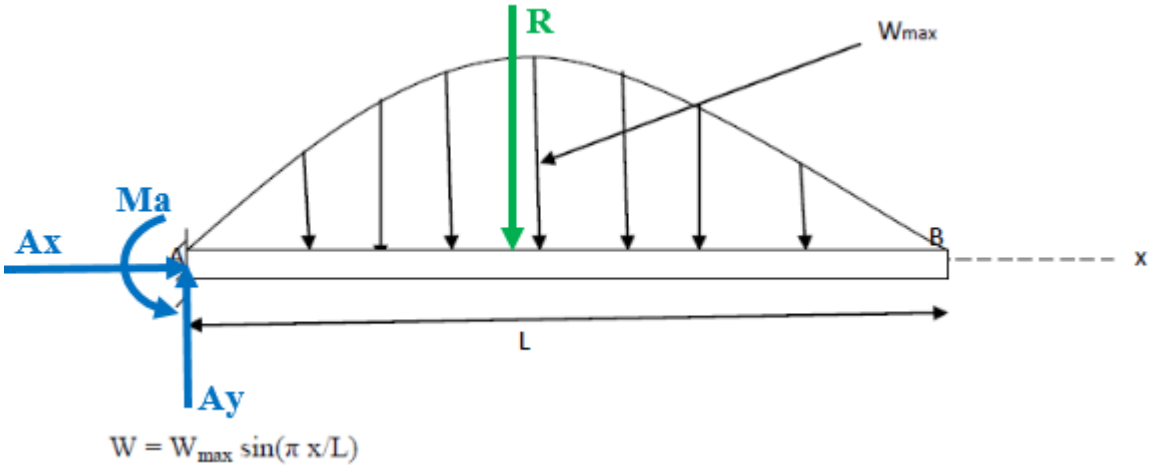
$W = W_{max} \sin(\pi\, x/L)$

Calcul de la résultante :

$$R = \int_0^L W dx = \int_0^L W_{max} \sin(\pi \frac{x}{L}) dx$$

$$R = int\left(Wmax \cdot \sin\left(\frac{\pi \cdot x}{L}\right), x = 0\ ..L\right);$$

$$R = \frac{2\,Wmax\,L}{\pi}$$

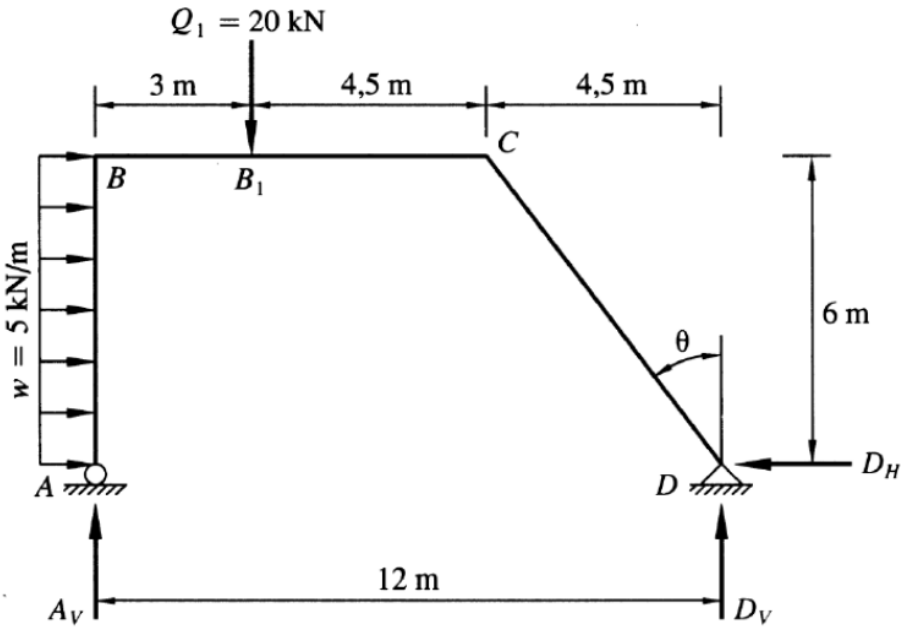


$$\sum Fy = 0 \Leftrightarrow Ay - R = 0$$

$$\Rightarrow Ay = \frac{2LW_{max}}{\pi}$$

$$Ma = R \times x = \frac{2LW_{max}}{\pi} \times \frac{L}{2} = \frac{L^2 W_{max}}{\pi}$$

Exercice 2 :



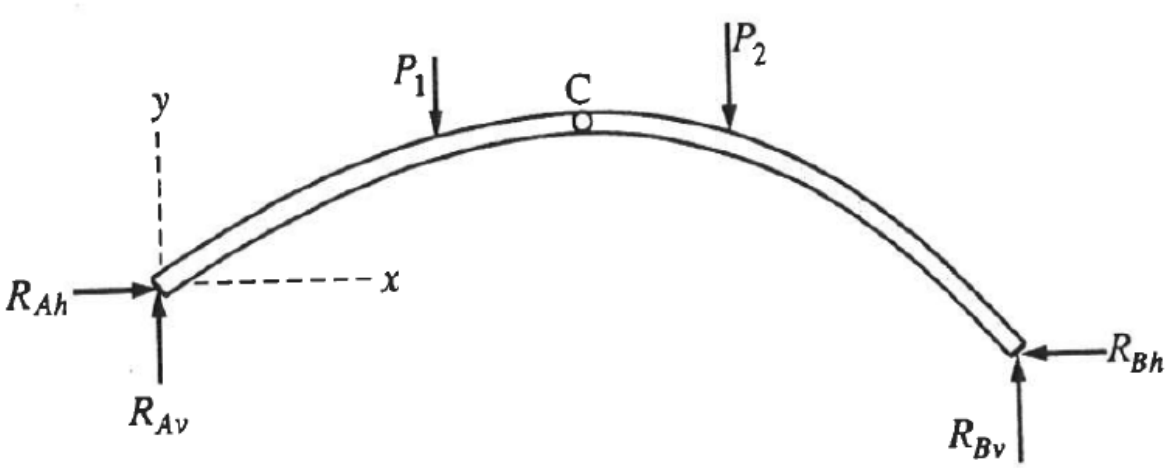
$$\sum Fx = 0 \Leftrightarrow w \times (6m) - D_H = 0 \Rightarrow D_H = 30\ kN$$

$$\sum M_D = 0 \Leftrightarrow Q_1 \times (4{,}5 + 4{,}5) - A_V \times 12 - w \times 6 \times \frac{6}{2} = 0 \Rightarrow A_V = 7{,}5\ kN$$

$$\sum Fy = 0 \iff A_V + D_V - Q_1 = 0 \implies \boxed{D_V = 12{,}5\ kN}$$

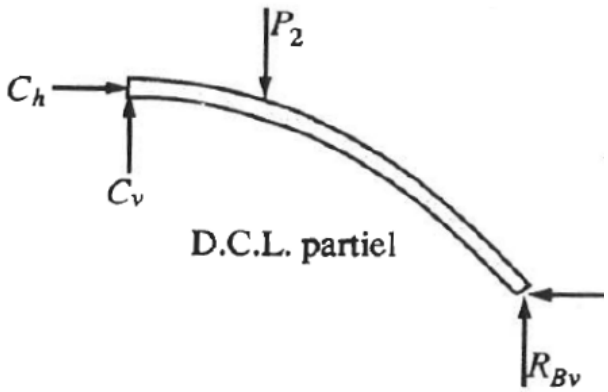
Exercice 3 :

DCL global :



$$(1): \sum Fx = 0 \Leftrightarrow R_{Ah} - R_{Bh} = 0$$
$$(2): \sum Fy = 0 \Leftrightarrow R_{Av} + R_{Bv} - P_1 - P_2 = 0$$
$$(3): \sum M_A = 0 \Leftrightarrow -R_{Bh} \times h + R_{Bv} \times L - P_1 \times a_1 - P_2 \times a_2 = 0$$

Il faut chercher une quatrième équation, donc on fait un DCL local sur la partie CB et on obtient :



$$(4): \sum M_C = 0$$
$$\Leftrightarrow -R_{Bh} \times (h + h')$$
$$+ R_{Bv} \times \frac{L}{2}$$
$$- P_2 \times (a_2 - a_C) = 0$$

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restart;
equ1 := Rah − Rbh = 0;
equ2 := Rav + Rbv − P1 − P2 = 0;
equ3 := Rbv·L − Rbh·h − P1·a1 − P2·a2 = 0;
equ4 := Rbv·l/2 − Rbh·(h + H) − P2·(a2 − ac) = 0;
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$$equ1 := Rah - Rbh = 0$$

$$equ2 := Rav + Rbv - P1 - P2 = 0$$

$$equ3 := Rbv\,L - P1\,a1 - P2\,a2 - Rbh\,h = 0$$

$$equ4 := \frac{Rbv\,l}{2} - Rbh\,(h + H) - P2\,(a2 - ac) = 0$$

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solve({equ4, equ3}, {Rbv, Rbh});
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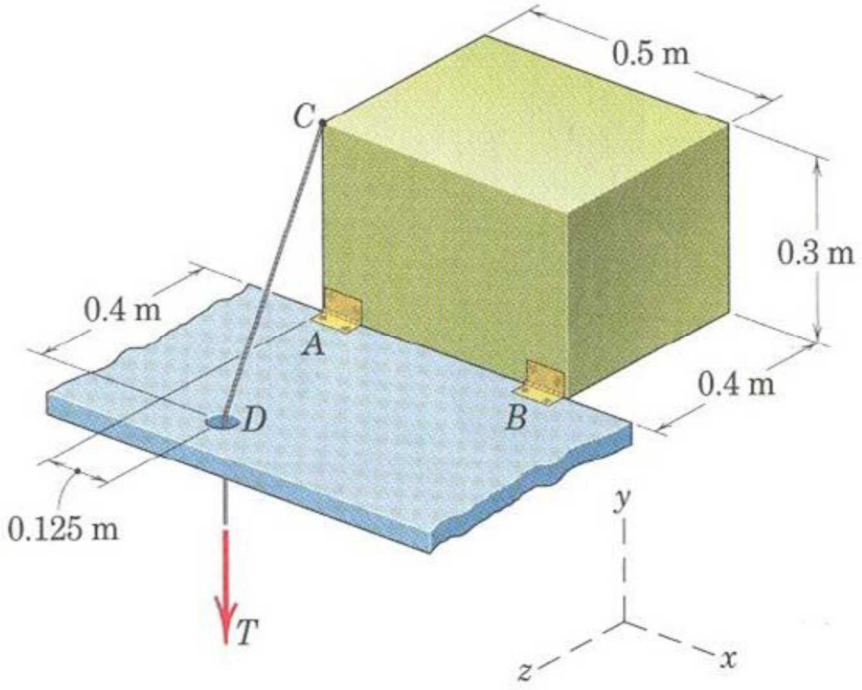
$$\left\{Rbh = -\frac{2\,L\,P2\,a2 - 2\,L\,P2\,ac - P1\,a1\,l - P2\,a2\,l}{2\,HL + 2\,L\,h - hl},\ Rbv = \frac{2\,(HP1\,a1 + HP2\,a2 + P1\,a1\,h + P2\,ac\,h)}{2\,HL + 2\,L\,h - hl}\right\}$$

Cherchons les réactions au point A :

$$Rah = -\frac{2\,L\,P2\,a2 - 2\,L\,P2\,ac - P1\,a1\,l - P2\,a2\,l}{2\,HL + 2\,L\,h - hl}$$

$$Rav = \frac{2\,HL\,P1 + 2\,HL\,P2 - 2\,HP1\,a1 - 2\,HP2\,a2 + 2\,L\,P1\,h + 2\,L\,P2\,h - 2\,P1\,a1\,h - P1\,hl - 2\,P2\,ac\,h - P2\,hl}{2\,HL + 2\,L\,h - hl}$$

Exercice 4 :



$$C = \begin{pmatrix} 0 \\ 0{,}3 \\ 0 \end{pmatrix} \; et \; D = \begin{pmatrix} 0{,}125 \\ 0 \\ 0{,}4 \end{pmatrix} \; donc \; \overrightarrow{CD} = 0{,}125\,\vec{\imath} - 0{,}3\,\vec{\jmath} + 0{,}4\,\vec{k}$$

$$et \; CD = \sqrt{0{,}125^2 + 0{,}3^2 + 0{,}4^2} = 0{,}515$$

$$\vec{T} = T\overrightarrow{\lambda_{CD}} = T\frac{\overrightarrow{CD}}{CD}$$

$$\Longrightarrow \vec{T} = T\left(\frac{0{,}125\,\vec{\imath} - 0{,}3\,\vec{\jmath} + 0{,}4\,\vec{k}}{0{,}515}\right) = (0{,}242 \times T)\,\vec{\imath} - (0{,}582 \times T)\vec{\jmath} + (0{,}776 \times T)\vec{k}$$

Afin de trouver la tension, on calcule la somme des moment suivant l'axe Ox :

$$\sum M_{Ox} = 0 \Leftrightarrow 0{,}3 \times Tz - 0{,}2 \times W = 0 \quad avec \; Tz = 0{,}776 \times T$$

$$\Rightarrow T = \frac{0{,}2 \times W}{0{,}3 \times 0{,}776} = \frac{0{,}2 \times 200 \times 9{,}81}{0{,}3 \times 0{,}776} = 1685{,}56\; N$$